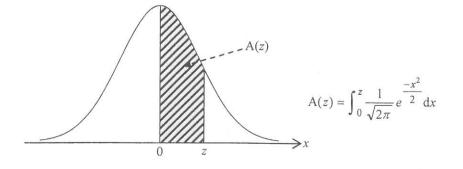
Standard Normal Distribution Table

Z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	.0359
0.1	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714	.0753
0.2	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103	.1141
0.3	.1179	.1217	.1255	.1293	.1331	.1368	.1406	.1443	.1480	.1517
0.4	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808	.1844	.1879
0.5	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.2224
0.6	.2257	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2517	.2549
0.7	.2580	.2611	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.2852
0.8	.2881	.2910	.2939	.2967	.2995	.3023	.3051	.3078	.3106	.3133
0.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545
1.7	.4554	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.4633
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4686	.4693	.4699	.4706
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4916
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986
3.0	.4987	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990	.4990
3.1	.4990	.4991	.4991	.4991	.4992	.4992	.4992	.4992	.4993	.4993
3.2	.4993	.4993	.4994	,4994	.4994	.4994	.4994	.4995	.4995	.4995
3.3	.4995	.4995	.4995	.4996	.4996	.4996	.4996	.4996	.4996	.4997
3.4	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4998
3.5	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998

Note: An entry in the table is the area under the standard normal curve between x = 0 and x = z ($z \ge 0$). Areas for negative values of z can be obtained by symmetry.



2019-DSE MATH EP M1

HONG KONG EXAMINATIONS AND ASSESSMENT AUTHORITY
HONG KONG DIPLOMA OF SECONDARY EDUCATION EXAMINATION 2019

MATHEMATICS Extended Part Module 1 (Calculus and Statistics) Question-Answer Book

8:30 am - 11:00 am (2% hours)This paper must be answered in English

INSTRUCTIONS

- (1) After the announcement of the start of the examination, you should first write your Candidate Number in the space provided on Page 1 and stick barcode labels in the spaces provided on Pages 1, 3, 5, 7, 9 and 11.
- (2) This paper consists of TWO sections, A and B.
- (3) Attempt ALL questions in this paper. Write your answers in the spaces provided in this Question-Answer Book. Do not write in the margins. Answers written in the margins will not be marked.
- (4) Graph paper and supplementary answer sheets will be supplied on request. Write your Candidate Number, mark the question number box and stick a barcode label on each sheet, and fasten them with string INSIDE this book.
- (5) Unless otherwise specified, all working must be clearly shown
- (6) Unless otherwise specified, numerical answers should be either exact or given to 4 decimal places.
- (7) No extra time will be given to candidates for sticking on the barcode labels or filling in the question number boxes after the 'Time is up' announcement.

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2019-DSE-MATH-EP(M1)-1

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(6 r	ar(3X+5).	Var(3X -	(+5) and	l k, E(3)	= 66 . Find	Var(<i>X</i>) =	It is given that
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(a)	By considering $P(A' \cap B')$, or otherwise, find $P(A)$.	
(b)	If A and B are independent, find $P(B)$.	
		(6 marks

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Answers written in the margins will not be marked.

Go on to the next page

(a)	Write down the mean and the variance of the number of draws for winning the big prize in a day
(b)	Within the first 4 draws in a day, are winning the big prize and not winning the big prize equal chance? Explain your answer.
(c)	Find the probability of not winning the big prize within the first 4 draws in each day for 5 day (7 mag)

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4.	offere	ch month, the probability that a store offers a discount to its products is 0.35 . If a discount is ed in a certain month, then the probability that the store makes a profit in that month is 0.7 wise, the probability of making a profit in that month is 0.28 .
	(a)	Find the probability that the store makes a profit in a certain month.
	(b)	Given that the store makes a profit in a certain month, find the probability that the store offers a discount in that month.
	(c)	Find the probability that the store makes a profit in at least 2 months out of 12 months. (6 marks)

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5.	Defin	$e f(x) = \frac{6-x}{x+3} \text{ for all } x > -3.$
	(a)	Prove that $f(x)$ is decreasing.
	(b)	Find $\lim_{x\to\infty} f(x)$ .
	(c)	Find the exact value of the area of the region bounded by the graph of $y = f(x)$ , the x-axis and the y-axis.  (6 marks)
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j.	(a)	Expand $e^{-18x}$ in ascending powers of x as far as the term in $x^2$ .	
	(b)	Let $n$ be a positive integer. If the coefficient of $x^2$ in the expansion of $e^{-18x}(1$ is $-38$ , find $n$ .	
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2019-DSE-MATH-EP(M1)-7

(a)	Find $\frac{dy}{dx}$ .
(b)	Someone claims that two of the tangents to $C$ are horizontal lines. Do you agree? Explain yanswer.
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2019-DSE-MATH-EP(M1)-8

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(a)	Express $7^{\frac{-1}{\ln 7}}$ in terms of $e$ .
(b)	By considering $\frac{d}{dx}(x7^{-x})$ , find $\int x7^{-x} dx$ .
(c)	Define $h(x) = x7^{-x}$ for all real numbers $x$ . It is given that the equation $h'(x) = 0$ has only
	one real root $\alpha$ . Find $\alpha$ . Also express $\int_0^{\alpha} h(x) dx$ in terms of $e$ .
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	9.	of 3	matche	of matches won by a basketball team in a season follows a Poisson distribution es per season. The points scored by the team in a match follows a normal distribution points and a standard deviation of 10 points.	
		(a)	Find t	the probability that the team wins fewer than 6 matches in a certain season.	(3 marks)
		(b)	Find t	the probability that the team scores higher than 70 points in a certain match.	(2 marks)
		(c)	match	eam receives a certificate if the team wins a match and scores more than 70 pm. The team is awarded a bonus in a certain season if the team reconstructed in that season.	
			(i)	Find the probability that the team wins exactly 3 matches in a certain so awarded a bonus in that season.	eason and is
_			(ii)	If the team wins exactly 4 matches in a certain season, find the probability is awarded a bonus in that season.	that the team
rusweis withen in the margins win not be marked			(iii)	Given that the team wins fewer than 6 matches in a certain season, find the that the team is awarded a bonus in that season.	
ווחו חב					(7 marks)
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distrib	oution v	the water consumption ( in $m^3$ ) of each family in a certain month follows a normal with a mean of $\mum^3$ and a standard deviation of $4m^3$ .
(a)	A sur	vey is conducted to estimate $\mu$ .
	(i)	A random sample of $16$ families is selected and their water consumptions (in $m^3$ ) in that month are recorded as follows:
		17 17 18 19 19 20 20 21 21 21 22 23 23 23 24 24
		Find a 95% confidence interval for $\mu$ .
	(ii)	Find the least sample size to be taken such that the width of a 99.5% confidence interval
		for $\mu$ is less than 3. (7 marks)
(b)	Supp	ose that $\mu = 20$ . If the water consumption of a family in that month lies between $18 \text{ m}^3$
	and	23 m ³ , the family is regarded as <i>ordinary</i> .
	(i)	Find the percentage of $ordinary$ families in city $H$ .
	(ii)	The families in city $H$ are randomly selected one by one and their water consumptions in that month are recorded. The recording stops when 3 ordinary families are found. Given that more than 6 families are selected in this recording process, find the probability that the water consumptions of exactly 9 families are recorded.  (6 marks)
\mass(\text{\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\text{\$\tin\}\$}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}}		

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11.	the sa	el factory has two machines, $P$ and $Q$ , for producing steel. The two machines start production at time. The manager of the factory models the rates of change of the amount of steel produced outsand tonnes per month) by $P$ and $Q$ respectively by
		$p(t) = 2t \ln(t^2 + 4)$ and $q(t) = \frac{4 \ln(2e^t + 1)}{e^{-t} + 2}$ $(0 \le t \le 4)$ ,
	steel p	e t is the number of months elapsed since the steel production begins. Denote the total amount of produced by P in the first 4 months by $\alpha$ thousand tonnes. Let $\alpha_1$ be the estimate of $\alpha$ by the trapezoidal rule with 4 sub-intervals.
	(a)	(i) Find $\alpha_1$ .
		(ii) Is $\alpha_1$ an over-estimate or an under-estimate? Explain your answer. (6 marks)
	(b)	Let $\beta$ thousand tonnes be the total amount of steel produced by $Q$ in the first 4 months.
		(i) Using the substitution $u = \ln(2e^t + 1)$ , find $\beta$ .
		(ii) The manager claims that the total amount of steel produced by $Q$ in the first 4 months exceeds 30% of the sum of the total amount of steel produced by $P$ and $Q$ in the first 4 months. Do you agree? Explain your answer.
		(6 marks)
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12.		c contains some water. Water is now leaking from the tank. Let $V  \text{m}^3$ be the volume of water nk. It is given that	in
		$V = \frac{64}{he^{kt} + 4} ,$	
	where	$t \ (\geq 0)$ is the number of hours elapsed since the leaking begins and $h$ and $k$ are constants.	
	(a)	Express $\ln\left(\frac{64}{V} - 4\right)$ as a linear function of $t$ . (1 mark	k)
	(b)	It is given that the graph of the linear function obtained in (a) passes through the origin and the point $(2,1)$ . Find	ne
		(i) $h$ and $k$ ,	
		(ii) $\frac{\mathrm{d}V}{\mathrm{d}t}$ ,	
		(iii) the value of $V$ when $\frac{dV}{dt}$ attains its least value.	-\
		(8 mark	
	(c)	The owner of the tank finds that $S = V^{\frac{2}{3}}$ , where $S \text{ m}^2$ is the wet total surface area of the tank	ζ.
		(i) Find the value of $\frac{dS}{dt}$ when $\frac{dV}{dt}$ attains its least value.	
		(ii) The owner claims that $\frac{dS}{dt}$ attains its least value when $\frac{dV}{dt}$ attains its least value. Is the	ne
		claim correct? Explain your answer. (4 marks	s)
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